

MSc Degree Examination
Branch II Physics
PH 211 – Classical mechanics

Duration: 3 hours

Maximum marks 75

Part A

Answer any five questions. Each question carries 3 marks

- 1 Show that phase trajectory of one dimensional harmonic oscillator is an ellipse.
- 2 State and explain Liouville's theorem
- 3 Represent Lorentz transformation in matrix form.
- 4 What are Euler angles
- 5 Explain cyclic coordinates with example.
- 6 Show that for a central force problem, angular momentum is a constant of motion.
- 7 Discuss the principle of least action
- 8 Define stable and unstable equilibrium.

5x3=15 marks

Part B

Answer three questions. Each question carries 15 marks

- 9
- | | |
|---|----|
| (a) State and explain Hamilton's principle | 5 |
| (b) Derive Lagrange's equations of motion from Hamilton's principle | 10 |
| OR | |
- 10
- | | |
|---|----|
| (a) Define Poisson bracket and derive its important properties | 5 |
| (b) Prove that Poisson bracket of two integrals of the equations of motion is also an integral of motion. | 10 |
- 15 marks
- 11
- | | |
|---|---|
| (a) Write down Hamilton Jacobi's equation and prove Jacobi's theorem | 6 |
| (b) Explain HJ method taking the example of a one dimensional harmonic oscillator | 9 |
| OR | |
- 12
- | | |
|--|---|
| (a) Explain generalised coordinates of a rigid body | 6 |
| (b) Discuss the problem of the motion of a heavy symmetrical top | 9 |
- 15 marks
- 13
- | | |
|---|---|
| (a) State the principle of equivalence and general principle of covariance | 6 |
| (b) Write down Einstein's equation of general relativity and explain its physical meaning | 9 |
| OR | |
- 14
- | | |
|---|---|
| (a) Explain linear and non linear systems | 5 |
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(b) Discuss the dynamics of Logistics map and explain its transition to chaos.

10

15 marks

Part C

Answer any three questions. Each question carries 5 marks

- 16 Obtain the equation of motion of a system of two masses, connected by an inextensible string passing over a small smooth pulley.
- 17 Determine the differential scattering cross section and the total scattering cross section for the scattering of a particle by a rigid elastic sphere.
- 18 A particle of mass m is attracted towards a given point by a force of the form $\frac{k}{r^2}$, where k is a constant. Write down the expression for the Hamiltonian of the system and derive Hamilton's equations of motion.
- 19 Show that the transformation $Q = q, P = p - \frac{1}{2}q^2$ is canonical
- 20 Determine the normal mode frequency of the Lagrangian, given by $L = \frac{1}{2}m\dot{q}^2 - \frac{1}{2}kq^2 + \frac{1}{4}kq^4$
- 21 Determine the length and the orientation of a rod of length 10 metres in a frame of reference which is moving with $0.6c$ velocity in a direction making 30° angle with the rod.

3x5=15 marks